

# Sign Conventions for EM Waves

EQUATION(S)	ENGINEERING (Negative Sign Convention)	$-j \leftrightarrow i$	PHYSICS/SCIENCE (Positive Sign Convention)												
Wave Propagating in + z Direction	$\cos(\omega t \mp kz)$ - forward wave $\exp(\mp jkz)$ + backward wave		$\cos(-\omega t \pm kz)$ - backward wave $\exp(\pm ikz)$ + forward wave												
Maxwell's Equations	$\nabla \times \vec{E} = -j\omega\vec{B}$ $\nabla \cdot \vec{D} = \rho_v$ $\vec{D} = \epsilon\vec{E}$ $\nabla \times \vec{H} = \vec{J} + j\omega\vec{D}$ $\nabla \cdot \vec{B} = 0$ $\vec{B} = \mu\vec{H}$		$\nabla \times \vec{E} = i\omega\vec{B}$ $\nabla \cdot \vec{D} = \rho_v$ $\vec{D} = \epsilon\vec{E}$ $\nabla \times \vec{H} = -\vec{J} - i\omega\vec{D}$ $\nabla \cdot \vec{B} = 0$ $\vec{B} = \mu\vec{H}$												
Wave Vector & Propagation Constant	$k = \beta - j\alpha$ $\gamma = jk = \alpha + j\beta$	$\alpha < 0$ gain (grow) $\alpha > 0$ loss (decay)	$k = \beta + i\alpha$ $\gamma = jk = -\alpha + j\beta$												
Complex $\mu, \epsilon$ and $n$	$\tilde{\epsilon} = \epsilon' - j\epsilon''$ $\tilde{\mu} = \mu' - j\mu''$ $\tilde{n} = n_o - j\kappa$	$n_o < 0$ neg. index $\kappa < 0$ gain (grow) $n_o > 0$ pos. index $\kappa > 0$ loss (decay)	$\tilde{n} = n_o + i\kappa$ $\tilde{\epsilon} = \epsilon' + i\epsilon''$ $\tilde{\mu} = \mu' + i\mu''$												
Lorentz Model	$\tilde{\epsilon}_r(\omega) = 1 + \frac{\omega_p^2}{\omega_0^2 - \omega^2 + j\omega\Gamma}$	$\Gamma < 0$ gain (grow) $\Gamma > 0$ loss (decay)	$\tilde{\epsilon}_r(\omega) = 1 + \frac{\omega_p^2}{\omega_0^2 - \omega^2 - i\omega\Gamma}$												
Fourier Transform	<table border="0" style="width: 100%;"> <tr> <td style="text-align: center;">Temporal</td> <td style="text-align: center;">Spatial</td> </tr> <tr> <td style="text-align: center;"><math>F(\omega) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} f(t)e^{-j\omega t} dt</math></td> <td style="text-align: center;"><math>F(k) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} f(x)e^{jkx} dx</math></td> </tr> <tr> <td style="text-align: center;"><math>f(t) = \int_{-\infty}^{+\infty} F(\omega)e^{j\omega t} d\omega</math></td> <td style="text-align: center;"><math>f(x) = \int_{-\infty}^{+\infty} F(k)e^{-jkx} dk</math></td> </tr> </table>	Temporal	Spatial	$F(\omega) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} f(t)e^{-j\omega t} dt$	$F(k) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} f(x)e^{jkx} dx$	$f(t) = \int_{-\infty}^{+\infty} F(\omega)e^{j\omega t} d\omega$	$f(x) = \int_{-\infty}^{+\infty} F(k)e^{-jkx} dk$		<table border="0" style="width: 100%;"> <tr> <td style="text-align: center;">Temporal</td> <td style="text-align: center;">Spatial</td> </tr> <tr> <td style="text-align: center;"><math>F(\omega) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} f(t)e^{i\omega t} dt</math></td> <td style="text-align: center;"><math>F(k) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} f(x)e^{-ikx} dx</math></td> </tr> <tr> <td style="text-align: center;"><math>f(t) = \int_{-\infty}^{+\infty} F(\omega)e^{-i\omega t} d\omega</math></td> <td style="text-align: center;"><math>f(x) = \int_{-\infty}^{+\infty} F(k)e^{ikx} dk</math></td> </tr> </table>	Temporal	Spatial	$F(\omega) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} f(t)e^{i\omega t} dt$	$F(k) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} f(x)e^{-ikx} dx$	$f(t) = \int_{-\infty}^{+\infty} F(\omega)e^{-i\omega t} d\omega$	$f(x) = \int_{-\infty}^{+\infty} F(k)e^{ikx} dk$
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