



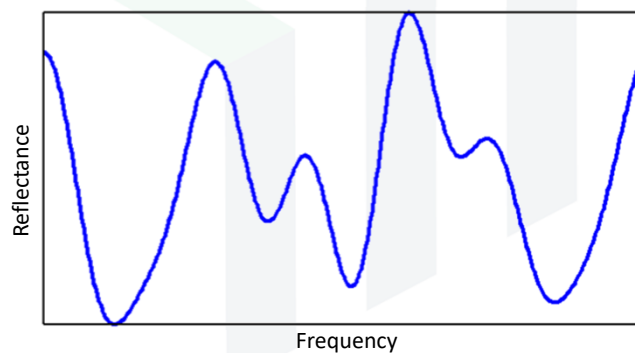
Computational Science:  
Computational Methods in Engineering

# The Rectangle Algorithm



## Goal of the Algorithm

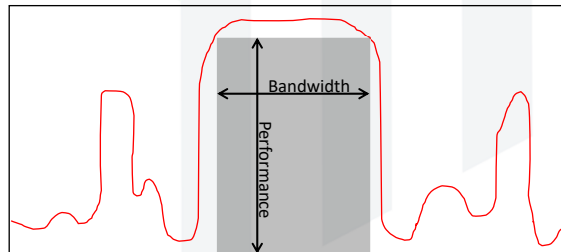
Suppose a broadband reflector is to be designed. An initial design is constructed, simulated and the reflectance calculated. Using a single quantity, what is the performance of this preliminary design?



## A Very Common Merit Function

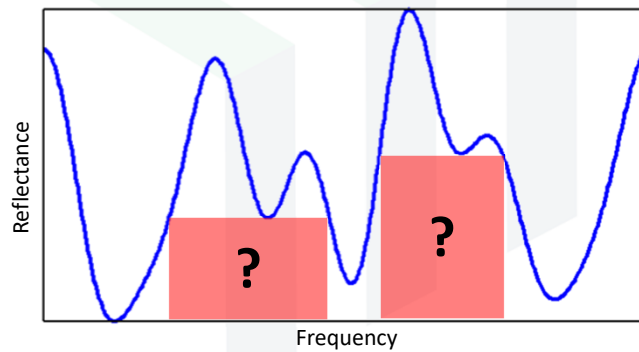
In electromagnetics, usually performance (i.e. reflectance here) is to be maximized over some bandwidth.

$$MF = (\text{Bandwidth}) \times (\text{Performance})$$



## The Rectangle Algorithm

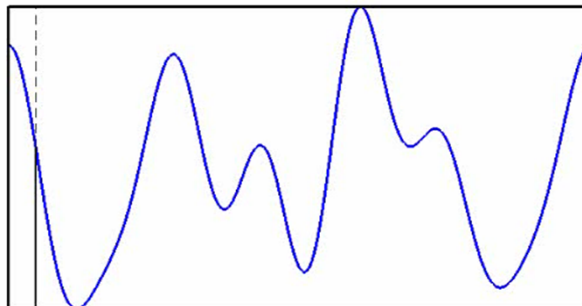
One possible merit function can be calculated by finding the biggest rectangle that fits under the reflectance curve. But...which rectangle is biggest?



## Steps in the Rectangle Algorithm

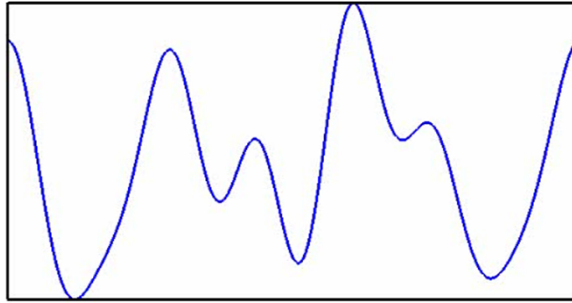
- Step 0 – Decide on a merit function.
- Step 1 – Simulate the spectrum of the device.
- Step 2 – Loop over all points in spectra.
  - i. Seek left to place left edge of rectangle.
  - ii. Seek right to place right edge of rectangle.
  - iii. Calculate merit function.
- Step 3 – Overall merit function is the area of the largest rectangle found in Step 2.

## Animation of Rectangle Construction



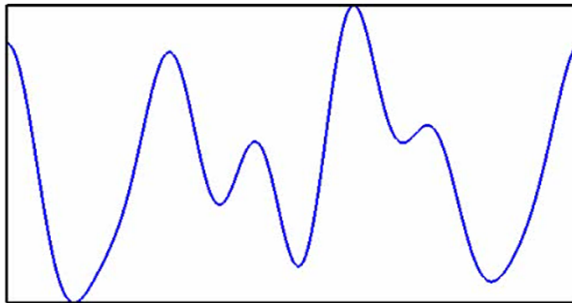
## Animation of the Rectangle Algorithm (1 of 3)

$$MF = w \cdot h$$



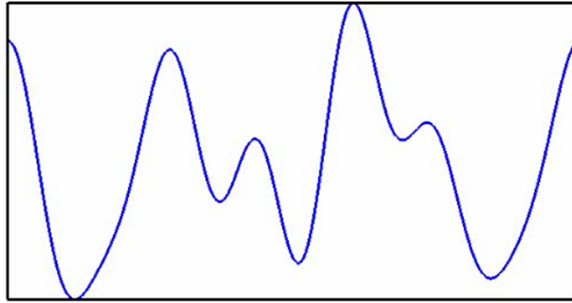
## Animation of the Rectangle Algorithm (2 of 3)

$$MF = \log(1 + w) \cdot h^3$$



## Animation of the Rectangle Algorithm (3 of 3)

$$MF = w^3 \cdot \log(1 + h)$$



## An Example Merit Function

Suppose it is desired to minimize transmission through a device where the application requires it to be broadband. You need both minimum transmission and wide bandwidth.

$$M \sim |T| \cdot BW$$

